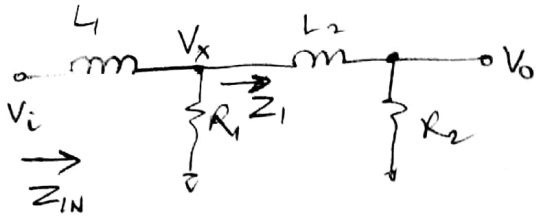


①



$$Z_1 = j\omega L_2 + R_2$$

$$Z_{IN} = j\omega L_1 + \frac{R_1(j\omega L_2 + R_2)}{R_1 + j\omega L_2 + R_2} \Rightarrow V_x = \frac{V_i}{Z_{IN}} \cdot \frac{R_1(j\omega L_2 + R_2)}{R_1 + j\omega L_2 + R_2}$$

$$= j\omega L_1 + \frac{R_1 Z_1}{R_1 + Z_1} = \frac{V_i}{Z_{IN}} \cdot \frac{R_1 Z_1}{R_1 + Z_1}$$

$$\Rightarrow V_x = \frac{V_i}{\left( \frac{j\omega L_1}{R_1 Z_1 / (R_1 + Z_1)} + 1 \right)} \quad V_o = \frac{V_x R_2}{Z_1}$$

$$\Rightarrow V_o = \frac{V_i}{Z_1 \left( \frac{j\omega L_1}{R_1 Z_1 / (R_1 + Z_1)} + 1 \right)} \quad R_2 = \frac{V_i R_2}{\frac{j\omega L_1 (R_1 + Z_1)}{R_1} + Z_1}$$

Denominator is:

$$\frac{j\omega L_1}{R_1} + \frac{j\omega L_1 R_2}{R_1} + \frac{\omega^2 L_1 L_2}{R_1} + j\omega L_2 + R_2 = \left( R_2 - \frac{\omega^2 L_1 L_2}{R_1} \right) + j \left[ \omega L_1 \left( 1 + \frac{R_2}{R_1} \right) + \omega L_2 \right]$$

$$= A e^{j\theta}$$

$$\text{where } A = \sqrt{\left( R_2 - \frac{\omega^2 L_1 L_2}{R_1} \right)^2 + \left[ \omega L_1 \left( 1 + \frac{R_2}{R_1} \right) + \omega L_2 \right]^2}$$

$$\theta = \tan^{-1} \left( \frac{\omega L_1 \left( 1 + \frac{R_2}{R_1} \right) + \omega L_2}{R_2 - \frac{\omega^2 L_1 L_2}{R_1}} \right)$$

$$\therefore V_o = \frac{V_i R_2}{A} e^{-j\theta}$$

For your problem:

(2)

$$L_1 = 0.1 \times 10^{-3} \text{ H} \quad R_1 = 10 \Omega \quad \omega = 5 \text{ kHz} \times 2\pi$$

$$L_2 = 0.2 \times 10^{-3} \text{ H} \quad R_2 = 50 \Omega$$

$$\begin{aligned} \omega L_1 \left(1 + \frac{R_2}{R_1}\right) + \omega L_2 &= 2\pi 5 \text{ k} \times 0.1 \text{ m} \left(1 + \frac{50}{10}\right) + 2\pi 5 \text{ k} \times 0.2 \text{ m} \\ &= 2\pi 5 \text{ k} \times 0.1 \text{ m} (1 + 5 + 2) \\ &= 2\pi 5 \text{ k} \times 0.8 \text{ m} = 25.13 \end{aligned}$$

$$R_2 - \frac{\omega^2 L_1 L_2}{R_1} = 50 - \frac{(2\pi 5 \text{ k})^2 \frac{0.02 \text{ m}}{10}}{10} = 48.03$$

$$\text{Magnitude} = V_i \frac{R_2}{A} = \frac{1 \times 50}{\sqrt{25.13^2 + 48.03^2}} = 0.922$$

$$\text{Angle} = \theta = \tan^{-1} \frac{25.13}{48.03} = 27.62^\circ$$

For the Book's problem:

$$L_1 = 1 \times 10^{-3} \text{ H} \quad R_1 = 10 \Omega \quad \omega = 5 \text{ kHz} \times 2\pi$$

$$L_2 = 2 \times 10^{-3} \text{ H} \quad R_2 = 50 \Omega$$

$$\omega L_1 \left(1 + \frac{R_2}{R_1}\right) + \omega L_2 = 2\pi 5 \text{ k} \times 1 \text{ m} \times 8 = 251.33$$

$$R_2 - \frac{\omega^2 L_1 L_2}{R_1} = 50 - \frac{(2\pi 5 \text{ k})^2 2 \text{ m}}{10} = -147.39$$

$$\text{Magnitude} = V_i \frac{R_2}{A} = \frac{1 \times 50}{\sqrt{251.33^2 + 147.39^2}} = 0.172$$

$$\text{Angle} = \theta = \tan^{-1} (251.33 / -147.39) = 120.39$$