

## Problema 1

Relação do prata calculado (por fora) usando a fonte Theory Of Surface Plasmon Resonance **OURO = Au = GOLD**

Obtain an expression for the electrical permittivity of a metal  $\epsilon(\omega)$  in the low-frequency regime in the free electron model. Using this expression determine the electrical permittivity of Au, Ag and Cu for a frequency of 10 GHz (microwave region). Tip get the necessary parameters for calculations from reported literature.

Constantes + Tabela:

$$n = 5.9 \cdot 10^{28}$$

$$\sigma(\text{ouro}) = 4.3 \cdot 10^7 \quad \rho = \frac{1}{4.3 \cdot 10^7} \rightarrow 23.2558 \cdot 10^{-9}$$

$$e^2 = \text{exponencial}$$

$$\omega = 2 \cdot \pi \cdot 1 \cdot 10^9 \rightarrow 2000000000 \cdot \pi$$

Fonte:

Design and Application of Plasmonic Devices - A Thesis

PLASMONICS: FUNDAMENTALS AND APPLICATIONS - STEFAN A. MAIER

Eq:

$$\epsilon(\omega) = 1 - \frac{(\omega p)^2}{\omega^2 + i \cdot \gamma \cdot \omega}$$

$$\epsilon(\omega) = 1 - \frac{5.94988 \cdot 10^{-4}}{(2000000000 \cdot \pi)^2 + i \cdot 4.09411 \cdot 10^{51} \cdot 2000000000 \cdot \pi} \rightarrow 1.0 + 23.1296 \cdot 10^{-66} \cdot i$$

Calculos:

$$\omega_p^2 = \frac{4 \cdot \pi \cdot q^2}{m} \quad \text{plasma frequency}$$

$$\omega_p = \sqrt{\frac{4 \cdot \pi \cdot (1.602 \cdot 10^{-19})^2}{9.11 \cdot 10^{-31}}} \rightarrow 594.988E-6$$

frequência do plasma:

$$\omega_p^2 = \frac{n \cdot e^2}{\epsilon_0 \cdot m}$$

$$\omega_p = \sqrt{\frac{5.9 \cdot 10^{28} \cdot e^2}{8.8541878176 \cdot 10^{-12} \cdot 9.11 \cdot 10^{-31}}} \rightarrow 232.481E33$$

$$\gamma = \frac{n \cdot e}{m \cdot e \cdot \sigma} \quad \text{Theory Of Surface Plasmon Resonance SPR}$$

$$\gamma = \frac{5.9 \cdot 10^{28} \cdot e^1}{9.11 \cdot 10^{-31} \cdot 4.3 \cdot 10^7} \rightarrow 4.09411E51$$

Estou usando a frequencia angular tradicional

Confirmar se esta ou outra forma

[https://www.brainkart.com/article/Solved-Problems--Conducting-Materials\\_6818/](https://www.brainkart.com/article/Solved-Problems--Conducting-Materials_6818/)

Verifica qual valor tal é o correto

$$\tau = \frac{\sigma \cdot m}{n \cdot e^2}$$

$$\tau = \frac{4.3 \cdot 10^7 \cdot 9.11 \cdot 10^{-31}}{5.9 \cdot 10^{28} \cdot e^2} \rightarrow 89.8557E-54$$

ou

Design and Application of Plasmonic Devices - A Thesis

$$\tau = \frac{m}{\rho \cdot n \cdot q^2}$$

$$\tau = \frac{9.11 \cdot 10^{-31}}{\frac{1}{4.3 \cdot 10^7} \cdot 5.9 \cdot 10^{28} \cdot (1.602 \cdot 10^{-19})^2} \rightarrow 25.8708 \times 10^{-15}$$

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Fonte: Optical properties of the metals Al, Co, Cu, Au, Fe, Pb, Ni, Pd, Pt, Ag, Ti, and W in the infrared and far infrared M. A. Ordal, L.

$$\omega\tau \left( cm^{-1} \right) = \frac{1}{2 \cdot \pi \cdot c \cdot \tau}$$

$$\omega\tau \left( cm^{-1} \right) = \frac{1}{2 \cdot \pi \cdot 300 \cdot 10^6 \cdot \tau}$$

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$$\sigma_0 = \frac{\omega p^2}{4 \cdot \pi \cdot \omega\tau}$$

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Metal	Electron density ( $m^{-3}$ )
Aluminum	$6.0 \times 10^{28}$
Copper	$8.5 \times 10^{28}$
Iron	$8.5 \times 10^{28}$
Gold	$5.9 \times 10^{28}$
Silver	$5.8 \times 10^{28}$

## Relações entre os termos da constante dielétrica e o índice de refração

Constante dielétrica      Índice de refração

$$\epsilon = \epsilon_1 + i\epsilon_2 = \tilde{n}^2$$

$$\tilde{n} = n + ik$$

$$\epsilon_1 = n^2 - k^2$$

$$\epsilon_2 = 2 \cdot n \cdot k$$

$$n^2 = \frac{\epsilon_1}{2} + \frac{1}{2} \cdot \sqrt{\epsilon_1^2 + \epsilon_2^2}$$

$$k = \frac{\epsilon_2}{2 \cdot n}$$