

Approximation with the characteristic function K

$$|S_{21}|^2 = \frac{1}{1+|K|^2} = \frac{1}{1+\left|\frac{F}{P}\right|^2} = \frac{|P|^2}{|F|^2+|P|^2}$$

$$|S_{11}|^2 = \frac{|K|^2}{1+|K|^2} = \frac{|F|^2}{|F|^2+|P|^2}$$

F, P : polynomials with real coefficients and no restrictions for the zeros

Zeros of F : reflection zeros $(|S_{21}|=1 \Rightarrow 0\text{dB} !!!)$

Zeros of P : transmission zeros $(|S_{21}|=0 \Rightarrow -\infty\text{dB})$

Example

Passband: 5.7 – 5.9

Return Loss: 22 dB

3 Resonators

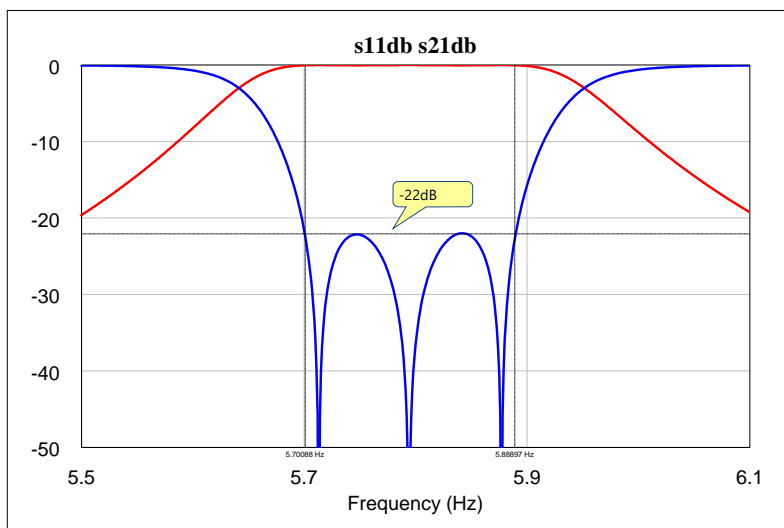
Reflections zeros: 5.713, 5.794, 5.877 $\rightarrow F(s) = (s^2 + \Omega_1^2) \cdot (s^2 + \Omega_2^2) \cdot (s^2 + \Omega_3^2)$

Transmission zeros: $P(s) = p_0 \cdot s^3$

"Rippel factor": $p_0 = 0.0215$

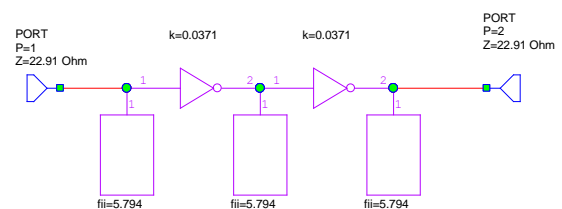
$$|K|^2 = \left| \frac{(-\Omega^2 + \Omega_1^2) \cdot (-\Omega^2 + \Omega_2^2) \cdot (-\Omega^2 + \Omega_3^2)}{p_0 \cdot (j\Omega)^3} \right|^2$$

Make a plot of s11db, s21db and tune the parameter (reflection zeros and p_0) leads to the result:



Next step: coupling matrix (normalized)

0	1.1376	0	0	0
1.1376	0	1.101	0	0
0	1.101	0	1.101	0
0	0	1.101	0	1.1376
0	0	0	1.1376	0



Next step: conversion to physical dimensions.