

# INPUT IMPEDANCE AND RESONANT FREQUENCY CHARACTERIZATION FOR FOLDED SLOT ANTENNAS THROUGH DOE TECHNIQUES<sup>1</sup>

Néstor D. López-Rivera\*, Rafael A. Rodríguez-Solís, Ph.D.  
Department of Electrical and Computer Engineering  
University of Puerto Rico  
Mayagüez, PR 00681-9042  
nestorl@ece.uprm.edu, rafaelr@ece.uprm.edu

## I. Introduction

This report is a continuation of [1], where an impedance matching technique for asymmetrical folded-slot antennas (FSAs) was introduced. Design of Experiment (DOE) techniques had been extensively used for improving the robustness of designs. In this work the effect of the design parameters on the FSA frequency response are characterized through DOE techniques. FSAs have recently been studied in [1-3]; folded-slot antennas on semi-infinite substrates are analyzed in [2], where FSA and Double Folded Slot Antennas (DFS) are characterized in terms of their radiation pattern and input impedance. FSAs on thin substrates have been analyzed using FDTD in [3], where the multiple-slot impedance engineering technique was developed.

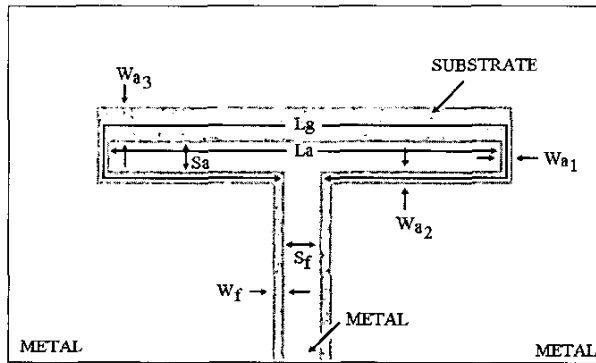


Figure 1. Schematic of a Folded Slot Antenna with its design parameters.

The FSAs considered in this research are fed through coplanar waveguide (CPW) and as shown in Figure 1, they have seven design parameters. These design parameters are  $L_a$ ,  $S_a$ ,  $W_{a1}$ ,  $W_{a2}$ ,  $W_{a3}$ , and the CPW feed ( $S_f$  and  $W_f$ ). For the proper characterization, we also have to consider the substrates width ( $h$ ) and its relative permittivity ( $\epsilon_r$ ). In [1] it was shown that the variation of  $W_{a3}$  was able to reduce the folded-slot's high input impedance to a desired value.

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## II. Methodology for the Characterization of the Folded Slot Antenna

To make the problem manageable, certain constraints were made. The substrate relative permittivity and its width were maintained constant with values of 3.48 and 0.762 mm respectively. Also, the antenna was fed through a 50  $\Omega$  CPW line obtained with a center conductor width of 3.657 mm and a slot width of 0.25 mm. The characterization was accomplished through DOE techniques. At specific values of  $L_a$ , a full  $2^4$  factorial design was used. The four factors observed for the design were  $S_a$ ,  $W_{a1}$ ,  $W_{a2}$  and  $W_{a3}$ , each with values of 0.25 mm or 1 mm. The parameter  $L_a$  has values of 23.497 mm, 13.357 mm and 10.157 mm. Each factorial design produced 16 different antennas for a total of 48 different simulations. Each factorial design was analyzed for the effects in our two responses; resonant frequency and input impedance at resonance for two different antenna resonances. The effects of the parameters are useful since they give us an insight on which variables or their interactions are the ones that mainly affect our response variables [4].

## III. Characterization of the Folded Slot Antenna

Figure 2 shows a usual impedance response for a FSA. The figure shows 4 resonant points. The trace begins at an open circuit for when direct current (DC) is applied and as the frequency begins to increase we move clockwise until the first resonance is reached, which occurs when the perimeter is approximately  $\lambda_g/2$ . This first resonance is characterized for having small impedance, almost a short circuit. As the frequency continues to increase, the impedance keeps moving clockwise until the second resonance is found, which occurs when the perimeter is approximately one guided wavelength ( $\lambda_g$ ). FSAs are mainly used at this resonance, with the impedance usually higher than 150  $\Omega$ . As the frequency increases, the third resonance appears when the FSAs' perimeter is around  $3\lambda_g/2$ . This resonance is characterized for having a low input impedance value. When the perimeter is approximately  $2\lambda_g$ , the impedance is approximately an open circuit. This work deals with the second and third resonances.

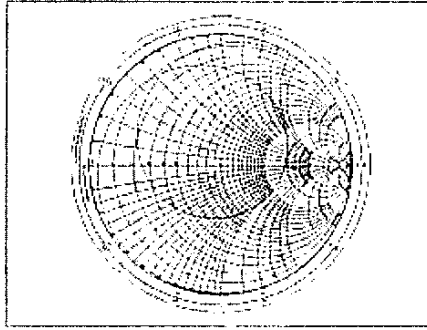


Figure 2. Usual Input Impedance response for a FSA.

As mentioned in the introduction, the values for  $L_a$  were set to 23.497 mm, 13.357 mm and 10.157 mm. By setting the parameters  $S_a$ ,  $W_{a1}$ ,  $W_{a2}$ , and  $W_{a3}$  to a value of 0.25 mm and for each of the respective  $L_a$  values the approximately resonant frequencies are 5 GHz, 9 GHz and 12 GHz. The factorial designs were analyzed for resonant frequency and input impedance at resonance for the  $\lambda_g$  and the  $3\lambda_g/2$  resonances. Table 1 shows the designs and the obtained

responses for the  $\lambda_g$  resonance, the results for the  $3\lambda_g/2$  resonance were omitted due to space limitations.

Table 1.  $2^4$  factorial designs and the two responses ( $f_{res}$  and  $Z_{in}$ ) for the  $\lambda_g$  resonance.

Design	$S_a$ (mm)	$W_{a1}$ (mm)	$W_{a2}$ (mm)	$W_{a3}$ (mm)	$L_a = 23.497$ mm		$L_a = 13.357$ mm		$L_a = 10.157$ mm	
					$f_{res}$ (GHz)	$Z_{in}$ ( $\Omega$ )	$f_{res}$ (GHz)	$Z_{in}$ ( $\Omega$ )	$f_{res}$ (GHz)	$Z_{in}$ ( $\Omega$ )
0	0.25	0.25	0.25	0.25	5.02	145.90	8.98	154.00	12.07	169.80
A	0.25	0.25	0.25	1	4.94	54.40	8.44	65.15	11.02	77.25
B	0.25	0.25	1	0.25	5.24	274.90	9.43	285.95	12.81	292.55
BA	0.25	0.25	1	1	5.17	134.65	9.04	149.45	11.98	157.15
C	0.25	1	0.25	0.25	4.70	159.95	8.05	184.70	10.55	214.10
CA	0.25	1	0.25	1	4.62	60.65	7.58	77.80	9.67	97.90
CB	0.25	1	1	0.25	4.91	254.30	8.44	322.75	10.99	350.30
CBA	0.25	1	1	1	4.84	147.95	8.05	177.90	10.90	204.45
D	1	0.25	0.25	0.25	4.94	153.35	8.65	162.25	11.45	173.50
DA	1	0.25	0.25	1	4.92	71.65	8.39	78.85	10.91	85.90
DB	1	0.25	1	0.25	5.15	252.40	9.10	261.55	12.03	275.20
DBA	1	0.25	1	1	5.10	142.00	8.89	144.30	11.72	142.40
DC	1	1	0.25	0.25	4.59	164.90	7.66	189.55	9.87	213.55
DCA	1	1	0.25	1	4.58	79.10	7.50	93.60	9.45	109.30
DCB	1	1	1	0.25	4.80	267.95	8.13	294.30	10.31	326.85
DCBA	1	1	1	1	4.77	153.70	7.92	175.00	10.12	190.75

#### a. Calculated effects at the $\lambda_g$ resonance

When the parameter  $L_a$  was fixed to 23.497 mm, as can be seen from Table 1, the resonating frequencies for the antennas vary between 4.583 GHz and 5.242 GHz. This change in the resonant frequency was due to the variation of parameters  $S_a$ ,  $W_{a1}$ ,  $W_{a2}$ , and  $W_{a3}$ . Nevertheless all the parameters and their interactions did not affect the response with the same intensity. Through DOE techniques we can conclude that the individual effects as well as the interaction between  $W_{a3}$  and  $S_a$  are the only ones which have a significant effect in our response ( $f_{res}$ ). The values for the calculated effects for the 3 different  $L_a$  values are presented in Table 2. On this range the effect that mainly cause the variations on  $f_{res}$  was the effect of parameter  $W_{a2}$  which negatively affect (reduce the resonant frequency as it increases) the resonant frequency. It is interesting to observe the positive effect of  $W_{a2}$  in the resonant frequency. It would be expected that increasing the antenna dimension will decrease the resonant frequency. The overall outcome of the effects increases as the value of the parameter  $L_a$  decreases, this because the expected resonant frequency increase and the antenna becomes more sensitive to its design parameters.

Table 2. Calculated effects for the  $\lambda_g$  resonant frequency.

$L_a$ (mm)	$W_{a1}$	$W_{a2}$	$W_{a3}$	$S_a$	$W_{a3} * S_a$
23.497	-0.025	0.100	-0.170	-0.037	0.013
13.357	-0.160	0.230	-0.470	-0.110	0.060
10.157	-0.270	0.370	-0.760	-0.260	-

Table 3 shows the calculated effects responsible for the variations in the input impedance at the respective resonant frequency. Supporting the work presented in [1] it is observed that the parameter  $W_{a3}$  has a large negative effect, which permits us to reduce the usually high input impedance at this resonance. It can also be seen that the parameter  $W_{a2}$  has a positive effect, which means that increasing  $W_{a2}$  will increase the input impedance at the resonant frequency. The parameter  $W_{a1}$  becomes significant as  $L_a$  decreases.

Table 3. Calculated effects for  $Z_{in}$  at the  $\lambda_g$  resonant frequency.

$L_a$ (mm)	$W_{a3}$	$W_{a2}$	$W_{a1}$	$W_{a3} * W_{a2}$
23.497	-51.85	46.12	-	-7.06
13.357	-55.81	50.33	13.38	-8.92
10.157	-59.42	49.90	20.84	-9.35

#### b. Calculated effects at the $3\lambda_g/2$ resonance

The calculated effects for the  $3\lambda_g/2$  resonant frequency and impedance at resonance are shown in Table 4 and in Table 5. As calculated and presented in Table 4, the only significant effects are the single effect of  $W_{a3}$ ,  $W_{a2}$  and  $S_a$ . In this case, for the three values of  $L_a$ , the dominant effect was that of  $W_{a3}$ . If we make  $L_a$  equals to 10.157 then the only significant effect is that of  $W_{a3}$ .

Table 4. Calculated effects for the resonant frequency

$L_a$ (mm)	$W_{a3}$	$W_{a2}$	$S_a$
23.497	-0.210	0.160	0.130
13.357	-0.270	0.240	0.180
10.157	-0.530	-	-

Table 5 shows the response for the input impedance at the  $3\lambda_g/2$  resonance. The positive effect for the  $W_{a2}$  dimension suggests that we can increase the short circuit like impedance on this resonance to a desired value. The negative interaction suggests that if we increase  $W_{a2}$  and decrease  $W_{a1}$  we can maximize this effect.

Table 5. Calculated effects for  $Z_{in}$  at the  $3\lambda_g/2$  resonant frequency.

$L_a$ (mm)	$W_{a2}$	$W_{a1}$	$W_{a1} * W_{a2}$
23.497	9.70	-2.40	-
13.357	12.19	-3.42	-2.17
10.157	13.64	-3.56	-2.55

## IV. Conclusions

This work presents a characterization of FSAs due to its design parameters through DOE techniques for the responses resonant frequency and input impedance at the resonant frequency for the  $\lambda_g$  and  $3\lambda_g/2$  resonances. The calculated effects are useful since they give us an insight on the effect of the design parameters on the antenna. It was verified that at the  $\lambda_g$  resonance the parameter  $W_{a3}$  has a great influence in decreasing the antenna input impedance. It was also found that increasing the dimension  $W_{a2}$  will increase the resonant frequency for the  $\lambda_g$  resonance, opposite as it would be expected. For last, in the  $3\lambda_g/2$  resonance we are able to increase the usually low input impedance by increasing the parameter  $W_{a2}$  making it a useful resonance.

## V. References

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