





One half analysis.

$$V_x = -g_{m1} \frac{V_{d1}}{2} \left( r_{ds1} \parallel \left[ \left( \frac{1}{g_{m3}} \parallel r_{ds3} \right) + \left( \frac{1}{g_{m7}} \parallel r_{ds7} \right) \right] \parallel \left[ \frac{1}{g_{m4}} \parallel r_{ds4} \right] + \left( \frac{1}{g_{m8}} \parallel r_{ds8} \right) \right]$$

$$= -g_{m1} \frac{V_{d1}}{2} \left( r_{ds1} \parallel \left( \frac{1}{g_{m3}} + \frac{1}{g_{m7}} \right) \parallel \left( \frac{1}{g_{m4}} + \frac{1}{g_{m8}} \right) \right)$$

Since  $\frac{1}{g_m}$  is much much smaller than  $r_{ds}$ .

Let us consider,

$$\Rightarrow \left( r_{ds1} \parallel \left( \frac{1}{g_{m3}} + \frac{1}{g_{m7}} \right) \parallel \left( \frac{1}{g_{m4}} + \frac{1}{g_{m8}} \right) \right)$$

$$\Rightarrow \left( r_{ds1} \parallel 2 \left( \frac{1}{g_{m3}} + \frac{1}{g_{m7}} \right) \right) \quad \text{as they are identical.}$$

$$\Rightarrow \left( 2 \frac{1}{g_{m3}} + \frac{1}{g_{m7}} \right) \quad \text{because}$$

So we get,

$$= -g_{m1} \frac{V_{d1}}{2} \left( 2 \frac{1}{g_{m3}} + \frac{1}{g_{m7}} \right)$$

$$V_x = -g_{m1} \left( \frac{g_{m7} + g_{m3}}{g_{m3} g_{m7}} \right) \cdot V_{d1}$$

$$V_{out1} = -g_{m3} \cdot V_x \cdot \frac{V_{d2}}{2} \cdot \left( r_{ds3} + \left( r_{ds1} \parallel \frac{1}{g_{m1}} \right) \parallel \left( r_{ds7} \parallel \frac{1}{g_{m7}} \right) \right)$$

$$\approx -g_{m3} \cdot V_x \cdot \frac{V_{d2}}{2}$$

consider,

$$\Rightarrow \left[ r_{ds3} + \left( r_{ds1} \parallel \frac{1}{g_{m1}} \right) \right] \parallel \left( r_{ds7} \parallel \frac{1}{g_{m7}} \right)$$

$$\Rightarrow \left[ r_{ds3} + \frac{1}{g_{m1}} \right] \parallel \left[ \frac{1}{g_{m7}} \right]$$

$$\Rightarrow \frac{1}{g_{m7}}$$

because  $\frac{1}{g_m}$  is much much smaller than any  $r_{ds}$ .

So, we have,

$$\approx -g_{m3} \cdot V_x \cdot \frac{V_{d2}}{2} \cdot \left( \frac{1}{g_{m7}} \right)$$

$$\approx -g_{m3} \cdot \frac{V_{d2}}{2} \cdot \left( \frac{1}{g_{m7}} \right) \cdot \left[ -g_{m1} \left( \frac{g_{m7} + g_{m3}}{g_{m7} \cdot g_{m3}} \right) \cdot V_{d1} \right]$$

$$V_{o1} = \frac{V_{d2}}{2} g_{m1} \frac{V_{d2}}{2} \cdot V_{d1} \cdot \frac{g_{m7} + g_{m3}}{(g_{m7})^2}$$